

# NCERT Solutions for Class 7 Maths Chapter 7

## **Congruence of Triangles Class 7**

Chapter 7 Congruence of Triangles Exercise 7.1, 7.2 Solutions

Exercise 7.1 : Solutions of Questions on Page Number : 137

Q1 : Complete the following statements:

(a) Two line segments are congruent if \_\_\_\_\_

(b) Among two congruent angles, one has a measure of 70°; the measure of the other angle is \_\_\_\_\_

(c) When we write  $\underline{A} = \underline{B}$ , we actually mean \_\_\_\_\_.

#### Answer :

(a) They have the same length

(b) 70°

(c) m  $A = m B_{2}$ 

#### Q2 :

Give any two real-life examples for congruent shapes.

#### Answer :

(i) Sheets of same letter pad (ii) Biscuits in the same packet

#### Q3 :

If ΔABC ≅ ΔFED under the correspondence ABC â†â€ FED, write all the Corresponding congruent parts of the triangles.

#### Answer :

If these triangles are congruent, then the corresponding angles and sides will be equal to each other.

 $\angle A \leftrightarrow E$ 

∠B ↔ <u>F</u>



 $\begin{array}{ccc} \angle & \angle & C \leftrightarrow D \\ \hline \overline{AB} \leftrightarrow \overline{FE} \\ \hline BC \leftrightarrow \overline{ED} \\ \hline \overline{CA} \leftrightarrow \overline{DF} \end{array}$ 

## Q4 :

If  $\Delta DEF \cong \Delta BCA$ , write the part(s) of  $\Delta BCA$  that correspond to

(i)  $_{\angle E}$  (ii)  $\overline{EF}$  (iii)  $_{\angle F}$  (iv)  $\overline{DF}$ 

(ii)

Answer :

(i) ∠C TA

(iii) ∠A

BA (iv)

Exercise 7.2 : Solutions of Questions on Page Number : 149 Q1

Which congruence criterion do you use in the following?

(a) Given: AC = DF AB = DE BC = EF

So,  $\triangle ABC \cong \triangle DEF$ 



(b) Given: ZX = RP RQ = ZY

∠ PRQ = <u>∦</u>ZY

So,  $\triangle PQR \cong \triangle XYZ$ 





(c) Given:∠ MLN = 4FGH MML = GFH

So,  $\Delta LMN \cong \Delta GFH$ 



(d) Given: EB = DB AE

= BC

∠ A = £ = 90°



Answer :

(a) SSS, as the sides of  $\triangle$ ABC are equal to the sides of  $\triangle$ DEF.

(b) SAS, as two sides and the angle included between these sides of  $\Delta$ PQR are equal to two sides and the angle included between these sides of  $\Delta$ XYZ. (c) ASA, as two angles and the side included between these angles of  $\Delta$ LMN are equal to two angles and the side included between these angles of  $\Delta$ GFH.

(d) RHS, as in the given two right-angled triangles, one side and the hypotenuse are respectively equal.

## Q2 :

You want to show that  $\triangle ART \cong \triangle PEN$ ,

(a) If you have to use SSS criterion, then you need to show



(i) AR = (ii) RT = (iii) AT =

(b) If it is given that *I* = № and you are to use SAS criterion, you need to have
(i) RT = and (ii) PN =

(c) If it is given that AT = PN and you are to use ASA criterion, you need to have (i) ? (ii) ?



## Answer :

(a) (i) AR = PE(ii) RT = EN(iii) AT = PN(b) (i) RT = EN(ii) PN = AT(c) (i)  $\angle ATR = P\underline{P}NE$  (ii) RAT = EPN $\angle \qquad \angle$ 

Q3 :

You have to show that  $\triangle AMP \cong AMQ$ .

In the following proof, supply the missing reasons.



-	Steps	-	Reasons
(i)	PM = QM	(i)	
(ii)	$\angle PMA = \angle QMA$	(ii)	
(iii)	AM = AM	(iii)	
(iv)	$\Delta AMP \cong \Delta AMQ$	(iv)	



#### Answer: (i)

Given

(ii) Given

- (iii) Common
- (iv) SAS, as the two sides and the angle included between these sides of  $\Delta$ AMP are equal to two sides and the angle included between these sides of  $\Delta$ AMQ.

Q4 :

In  $\triangle ABC$ ,  $\angle A = 30^{\circ}$ ,  $4 = 40^{\circ}$  and  $C = 110^{\circ}$ 

In  $\triangle PQR$ ,  $\angle P = 30^{\circ}$ ,  $\overleftarrow{Q} = 40^{\circ}$  and  $\overrightarrow{R} = 110^{\circ}$  A student says that  $\triangle ABC \cong \triangle PQR$  by AAA

congruence criterion. Is he justified? Why or why not?

#### Answer :

No. This property represents that these triangles have their respective angles of equal measure. However, this gives no information about their sides. The sides of these triangles have a ratio somewhat different than 1:1. Therefore, AAA property does not prove the two triangles congruent.

#### Q5 :

In the figure, the two triangles are congruent.



## The corresponding parts are marked. We can write $\Delta \text{RAT}$ ?



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#### Answer :

It can be observed that,

∠RAT = WON

∠ART = QWN AR = OW

Therefore,  $\Delta RAT \cong \Delta WON$ , by ASA criterion.

## Q6 :

Complete the congruence statement:

#### ΔBCA ≅?



Answer :

Given that, BC = BT TA = CA BA is common. Therefore,  $\Delta$ BCA  $\cong \Delta$ BTA

Similarly, PQ = RS TQ = QS PT = RQ

Therefore,  $\Delta QRS \cong \Delta TPQ$ 



#### Q7:

In a squared sheet, draw two triangles of equal areas such that

(i) The triangles are congruent.

(ii) The triangles are not congruent.

What can you say about their perimeters?

#### Answer :

(i)



Here,  $\Delta ABC$  and  $\Delta PQR$  have the same area and are congruent to each other also. Also, the perimeter of both the triangles will be the same.

(ii)



Here, the two triangles have the same height and base. Thus, their areas are equal. However, these triangles are not congruent to each other. Also, the perimeter of both the triangles will not be the same.

#### Q8 :

If ΔABC and ΔPQR are to be congruent, name one additional pair of corresponding parts. What criterion did you use?



Answer : BC = QR

 $\triangle ABC \cong \triangle PQR$  (ASA criterion)



### Q9 : Explain, why

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ΔABC ΔFED



#### Answer :

Given that, ABC = PED (1) ∠ BAC =

∠ EFD (2)

The two angles of  $\triangle$ ABC are equal to the two respective angles of  $\triangle$ FED. Also, the sum of all interior angles of a triangle is 180°.

Therefore, third angle of both triangles will also be equal in measure. BCA = EDF(3)

Also, given that, BC = ED (4) By using equation (1), (3), and (4), we obtain

 $\triangle ABC \cong \triangle FED$  (ASA criterion)