

<u>Class IX</u> Chapter 1 –

Number Sustems Maths

Exercise 1.1 Question

Is zero a rational number? Can you write it in the form q, where p and q are integers \neq 0?

 \underline{p}

and q

Answer:

Yes. Zero is a rational number as it can be represented as $\frac{0}{1}$ or $\frac{0}{2}$ or $\frac{0}{3}$ etc.

Question 2:

Find six rational numbers between 3 and 4.

Answer:

There are infinite rational numbers in between 3 and 4.

$$\frac{24}{8}$$
 and $\frac{32}{8}$

respectively.

3 and 4 can be represented as

Therefore, rational numbers between 3 and 4 are $\frac{25}{8}, \frac{26}{8}, \frac{27}{8}, \frac{28}{8}, \frac{29}{8}, \frac{30}{8}$

Question 3:



www.eduinput.co Find five rational between Answer:	m $\frac{3}{5}$ and $\frac{4}{5}$		numbers
There are infinite between .	<u> </u>	rational	numbers
Delween.			
$\frac{3}{5} = \frac{3 \times 6}{5 \times 6} = \frac{18}{30}$ $\frac{4}{5} = \frac{4 \times 6}{5 \times 6} = \frac{24}{30}$	$\frac{\frac{3}{5} \text{ and } \frac{4}{5}}{\frac{3}{5} \text{ and } \frac{4}{5}}$ numbers between		
Therefore, rational are			

Therefore, rational are $\frac{19}{30}, \frac{20}{30}, \frac{21}{30}, \frac{22}{30}, \frac{23}{30}$ Question 4:

State whether the following statements are true or false. Give reasons for your answers.

- (i) Every natural number is a whole number.
- (ii) Every integer is a whole number.
- (iii) Every rational number is a whole number.

Answer:

- (i) True; since the collection of whole numbers contains all natural numbers.
- (ii) False; as integers may be negative but whole numbers are positive. For example: −3 is an integer but not a whole number.

(iii) False; as rational numbers may be fractional but whole numbers may not be. For

example: $\frac{1}{5}$ is a rational number but not a whole number.



Exercise 1.2 Question 1:

State whether the following statements are true or false. Justify your answers.

- (i) Every irrational number is a real number.
- (ii) Every point on the number line is of the form \sqrt{m} , where m is a natural number.
- (iii) Every real number is an irrational number.

Answer:

- (i) True; since the collection of real numbers is made up of rational and irrational numbers.
- (ii) False; as negative numbers cannot be expressed as the square root of any other number.
- (iii)False; as real numbers include both rational and irrational numbers. Therefore, every real number cannot be an irrational number.



Question 2:

Are the square roots of all positive integers irrational? If not, give an example of the square root of a number that is a rational number.

Answer:

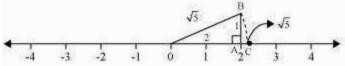
If numbers such as $\sqrt{4} = 2$, $\sqrt{9} = 3$ are considered, Then here, 2 and 3 are rational numbers. Thus, the square roots of all positive integers are not irrational.

Question 3: 15

Answer:

We know that,

 $\sqrt{5} = \sqrt{(2)^2 + (1)^2}$ Show howAnd, can be represented on the number line.



Mark a point 'A' representing 2 on number line. Now, construct AB of unit length perpendicular to OA. Then, taking O as centre and OB as radius, draw an arc intersecting number line at C.

C is representing $\sqrt{5}$.



www.eduinput.com has: (i) $\frac{36}{100}$ (ii) $\frac{1}{11}$ (iii) $4\frac{1}{8}$ (iv) $\frac{3}{13}$ (v) $\frac{2}{11}$ (vi) $\frac{329}{400}$ Answer: 36 = 0.36(i) 100 Terminating <u>1</u> = 0.090909..... (ii) 11 = 0.09Non-terminating repeating $4\frac{1}{8} = \frac{33}{8} = 4.125$ (iii) Terminating $\frac{3}{10} = 0.230769230769.... = 0.230769$ (iv) 13 Non-terminating repeating = 0.18181818...... = 0.18 (v) 11 Non-terminating repeating 329 = 0.8225 (vi) 400 Terminating = 0.142857Question 2: You know that 2 3 4 5 6 7'7'7'7 Exercise 1.3 Question 1:

Write the following in decimal form and say what kind of decimal expansion each . Can you predict what the decimal expansion of are, without actually doing the long division? If so, how?



www.eduinput.com Yes. It can be done as follows. $\frac{2}{7} = 2 \times \frac{1}{7} = 2 \times 0.142857 = 0.285714$, where p and q are integers and q ≠ 0. $\frac{3}{7} = 3 \times \frac{1}{7} = 3 \times 0.142857 = 0.428571$ 10x = 6 + x $\frac{4}{7} = 4 \times \frac{1}{7} = 4 \times 0.\overline{142857} = 0.\overline{571428}$ $\frac{5}{7} = 5 \times \frac{1}{7} = 5 \times 0.\overline{142857} = 0.\overline{714285}$ $\frac{6}{7} = 6 \times \frac{1}{7} = 6 \times 0.\overline{142857} = 0.\overline{857142}$ 9x = 6 $x = \frac{2}{3}$ (ii) $0.\overline{47} = 0.4777....$ Question 3: <u>p</u> Let x = 0.777... 10x = 7.777... q10x = 7 + xExpress the following in the form $x = \frac{7}{9}$ (i) $0.\overline{6}$ (ii) $0.4\overline{7}$ (iii) $0.\overline{001}$ $\frac{4}{10} + \frac{0.777...}{10} = \frac{4}{10} + \frac{7}{90}$ Answer: (i) $0.\overline{6} = 0.666...$ $=\frac{36+7}{90}=\frac{43}{90}$ Let x = 0.666...10x = 6.666...(iii) 0.001 = 0.001001... Let x = 0.001001...1000x = 1.001001...1000x = 1 + x1 [Hint: Study the remainders while finding the value of 7 carefully.] Answer:

 $x = \frac{1}{999}$

999x = 1

Question 4:

p

Express 0.999999...in the form q. Are you surprised by your answer? With your teacher and classmates discuss why the answer makes sense.



Answer:

Let x = 0.9999...10x = 9.9999...10x = 9 + x

9x = 9x =

1

Question 5:

What can the maximum number of digits be in the repeating block of digits in the decimal $\frac{1}{17}$ expansion of $\frac{1}{17}$? Perform the division to check your answer.

1

p

Answer:

It can be observed that, $\frac{1}{17} = 0.0588235294117647$

There are 16 digits in the repeating block of the decimal expansion of 17 .

Question 6:

Look at several examples of rational numbers in the form $\frac{p}{q}$ (q \neq 0), where p and q are integers with no common factors other than 1 and having terminating decimal representations (expansions). Can you guess what property q must satisfy?

Answer:

Terminating decimal expansion will occur when denominator q of rational number q is either of 2, 4, 5, 8, 10, and so on...



$$\frac{9}{4} = 2.25$$
$$\frac{11}{8} = 1.375$$
$$\frac{27}{5} = 5.4$$

It can be observed that terminating decimal may be obtained in the situation where prime factorisation of the denominator of the given fractions has the power of 2 only or 5 only or both.

Question 7:

Write three numbers whose decimal expansions are non-terminating non-recurring. Answer:

3 numbers whose decimal expansions are non-terminating non-recurring are as follows.

0.505005000500005000005...

0.7207200720007200007200000... 0.080080008000080000080...

Question 8:

 $\frac{9}{11}$

5

Find three different irrational numbers between the rational numbers and Answer:

$$\frac{5}{7} = 0.\overline{714285}$$
$$\frac{9}{11} = 0.\overline{81}$$

3 irrational numbers are as follows.

0.73073007300073000073...

0.7507500750007500075... 0.7907900790007900079...

Question 9:



www.eduinput.com Classify the following numbers as rational or irrational:

(i)
$$\sqrt{23}$$
 (ii) $\sqrt{225}$ (iii) 0.3796
(iv) 7.478478 (v) 1.10100100010001...
(i) $\sqrt{23} = 4.79583152331$...

As the decimal expansion of this number is non-terminating non-recurring, therefore, it is an irrational number.

(ii)
$$\sqrt{225} = 15 = \frac{15}{1}$$

<u>p</u>

It is a rational number as it can be represented in q form.

(iii) 0.3796

As the decimal expansion of this number is terminating, therefore, it is a rational number.

As the decimal expansion of this number is non-terminating recurring, therefore, it is a rational number.

(v) 1.10100100010000 ...

As the decimal expansion of this number is non-terminating non-repeating, therefore, it is an irrational number.



Exercise 1.4 Question

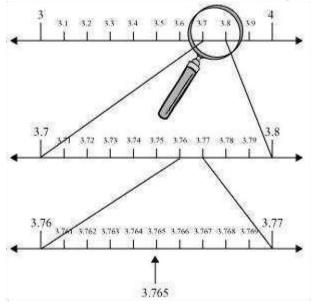
1:

Visualise 3.765 on the number line using successive magnification.



Answer:

3.765 can be visualised as in the following steps.



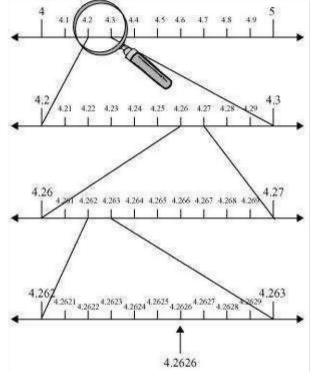
Question 2:

Visualise 4.26 on the number line, up to 4 decimal places.

Answer:

4.26 = 4.2626...

4.2626 can be visualised as in the following steps.





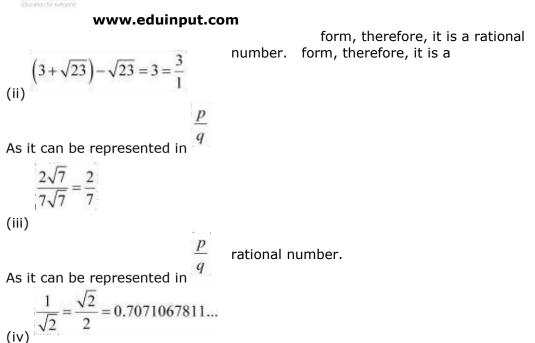
Exercise 1.5 Question 1:

1Classify the following numbers as rational or irrational:

(i)
$$2-\sqrt{5}$$
 (ii) $(3+\sqrt{23})-\sqrt{23}$ (iii) $\frac{2\sqrt{7}}{7\sqrt{7}}$
(iv) $\frac{1}{\sqrt{2}}$ (v) 2n
Answer:
(i) $2-\sqrt{5}$ = 2 - 2.2360679...
= - 0.2360679...

As the decimal expansion of this expression is non-terminating non-recurring, therefore, it is an irrational number.





As the decimal expansion of this expression is non-terminating non-recurring,

therefore, it is an irrational number. (v) $2\pi = 2(3.1415 ...)$

= 6.2830 ...

As the decimal expansion of this expression is non-terminating non-recurring, therefore,

it is an irrational number.



Question 2:

Simplify each of the following expressions:

(i)
$$\frac{(3+\sqrt{3})(2+\sqrt{2})}{(\sqrt{5}+\sqrt{2})^{2}}$$
(ii)
$$\frac{(3+\sqrt{3})(3-\sqrt{3})}{(\sqrt{5}-\sqrt{2})(\sqrt{5}+\sqrt{2})}$$
(iii)

Answer:

Recall, π is defined as the ratio of the circumference (say c) of a circle to its diameter

(say d). That is, $\pi = \frac{c}{d}$. This seems to contradict the fact that π is irrational. How will you resolve this contradiction?

Answer:

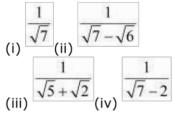
There is no contradiction. When we measure a length with scale or any other instrument, we only obtain an approximate rational value. We never obtain an exact value. For this reason, we may not realise that either c or d is irrational. Therefore,



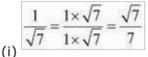
the $\frac{c}{d}$ fraction is irrational. Hence, π is irrational. Question 4: number $\sqrt{9.3}$ line. Answer:

Mark a line segment OB = 9.3 on number line. Further, take BC of 1 unit. Find the midpoint

D of OC and draw a semi-circle on OC while taking D as its centre. Draw a

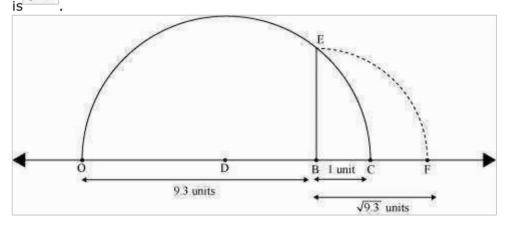


Answer:



perpendicular to line OC passing through point B. Let it intersect the semi-circle at E.

Taking B as centre and BE as radius, draw an arc in tersecting number line at F. BF $\sqrt{9.3}$.



Question 5:

Rationalise the denominators of the following:



$$\frac{1}{\sqrt{7} - \sqrt{6}} = \frac{1}{(\sqrt{7} + \sqrt{6})} \frac{\sqrt{7} + \sqrt{6}}{(\sqrt{7} - \sqrt{6})(\sqrt{7} + \sqrt{6})}$$
(ii)

$$= \frac{\sqrt{7} + \sqrt{6}}{(\sqrt{7})^2 - (\sqrt{6})^2}$$

$$= \frac{\sqrt{7} + \sqrt{6}}{7 - 6} = \frac{\sqrt{7} + \sqrt{6}}{1} = \sqrt{7} + \sqrt{6}$$
(iii)

$$= \frac{1}{\sqrt{5} + \sqrt{2}} = \frac{1}{(\sqrt{5} + \sqrt{2})(\sqrt{5} - \sqrt{2})}$$
(iii)

$$= \frac{\sqrt{5} - \sqrt{2}}{(\sqrt{5})^2 - (\sqrt{2})^2} = \frac{\sqrt{5} - \sqrt{2}}{5 - 2}$$

$$= \frac{\sqrt{5} - \sqrt{2}}{3}$$
(iv)

$$= \frac{\sqrt{7} + 2}{(\sqrt{7})^2 - (2)^2}$$

$$= \frac{\sqrt{7} + 2}{7 - 4} = \frac{\sqrt{7} + 2}{3}$$

Exercise 1.6 Question 1:

Find:

$$64^{\frac{1}{2}}$$
 $32^{\frac{1}{5}}$ $125^{\frac{1}{3}}$



www.eduinput.com (i) $9^{\frac{3}{2}} = (3^2)^{\frac{3}{2}}$ $=3^{2\times\frac{3}{2}}$ $\left[\left(a^{m}\right)^{n}=a^{mn}\right]$ Find: (i) $9^{\frac{3}{2}}$ (ii) $32^{\frac{2}{5}}$ (iii) $16^{\frac{3}{4}}$ $=3^3 = 27$ (ii) (iv) $\frac{125^{\frac{-1}{3}}}{125^{\frac{-1}{3}}}$ $(32)^{\frac{2}{5}} = (2^5)^{\frac{2}{5}}$ Answer: $=2^{5\times\frac{2}{5}}$ Answer: $\left[\left(a^{m}\right)^{n}=a^{mn}\right]$ (i) $=2^{2}=4$ $64^{\frac{1}{2}} = (2^6)^{\frac{1}{2}}$ $\left[\left(a^{m}\right)^{n}=a^{mn}\right]_{\left(16\right)^{\frac{3}{4}}=\left(2^{4}\right)^{\frac{3}{4}}}^{(\text{iii})}$ $=2^{6\times\frac{1}{2}}$ $=2^3=8$ $=2^{4\times\frac{3}{4}}$ $\left[\left(a^{m}\right)^{n}=a^{mn}\right]$ $\frac{(ii)}{32^{\frac{1}{5}} = \left(2^{5}\right)^{\frac{1}{5}}}$ $=2^3=8$ $\left[\left(a^{m}\right)^{n} = a^{mn}\right]_{(125)^{\frac{-1}{3}} = \frac{1}{(125)^{\frac{1}{3}}}}^{(125)^{\frac{-1}{3}}}$ $=(2)^{5\times\frac{1}{5}}$ $\left[a^{-m}=\frac{1}{a^{m}}\right]$ $=2^{1}=2$ $=\frac{1}{\left(5^3\right)^{\frac{1}{3}}}$ (iii) $(125)^{\frac{1}{3}} = (5^3)^{\frac{1}{3}}$ $\left[\left(a^m\right)^n = a^{mn}\right] \qquad \qquad = \frac{1}{5^{3 \times \frac{1}{3}}}$ $\left[\left(a^{m}\right)^{n}=a^{mn}\right]$ $=5^{3\times\frac{1}{3}}$ $=5^{1}=5$ $=\frac{1}{\epsilon}$

Question 2:

Question 3:



Simplify:

(i)
$$2^{\frac{2}{3}} \cdot 2^{\frac{1}{5}}$$
 (ii) $\left(\frac{1}{3^{3}}\right)^{7}$ (iii) $\frac{11^{2}}{11^{\frac{1}{4}}}$
(iv) $7^{\frac{1}{2}} \cdot 8^{\frac{1}{2}}$

Answer:

(i)	
$2^{\frac{2}{3}} \cdot 2^{\frac{1}{5}} = 2^{\frac{2}{3} + \frac{1}{5}}$	$\left[a^{m}.a^{n}=a^{m+n}\right]$
$=2^{\frac{10+3}{15}}=2^{\frac{13}{15}}$	~ ~

$\left(\frac{1}{3^3}\right)^7 = \frac{1}{3^{3\times 7}}$	$\left[\left(a^{m}\right)^{n}=a^{mn}\right]$
$=\frac{1}{3^{21}}$	
$=3^{-21}$	$\left[\frac{1}{a^m}=a^{-m}\right]$

(iii)

$\frac{11^{\frac{1}{2}}}{1} = 11^{\frac{1}{2}-\frac{1}{4}}$	$\left[\frac{a^m}{a} = a^{m-n}\right]$
$11^{\frac{1}{4}}$	[<i>a</i> "]
$=11^{\frac{2-1}{4}}=11^{\frac{1}{4}}$	

(iv)

1.1. 1	
$7^{\overline{2}}.8^{\overline{2}} = (7 \times 8)^{\overline{2}}$	$[a^m.b^m=(ab)^m]$
$=(56)^{\frac{1}{2}}$	