

Class IX Chapter 7 – Triangles

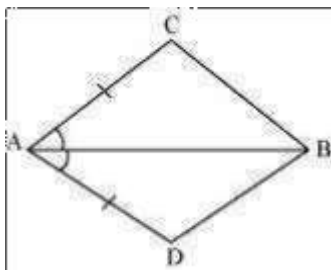
Maths

Exercise 7.1 Question

1:

In quadrilateral ACBD, $AC = AD$ and AB bisects $\angle A$ (See the given figure). Show that

$\triangle ABC \cong \triangle ABD$



Answer: $\triangle ABC \cong \triangle ABD$. What can you say about BC and BD ?

In $\triangle ABC$ and $\triangle ABD$,

$AC = AD$ (Given)

$\angle CAB = \angle DAB$ (AB bisects $\angle A$)

$AB = AB$ (Common)

\therefore

$\therefore \triangle ABC \cong \triangle ABD$ (By SAS congruence rule)
 $BC = BD$ (By CPCT)

Therefore, BC and BD are of equal lengths.

Question 2:

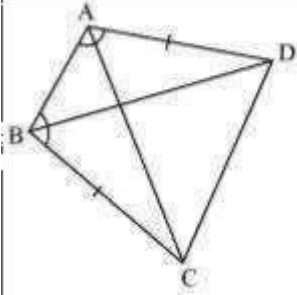
$ABCD$ is a quadrilateral in which $AD = BC$ and $\angle DAB = \angle CBA$ (See the given figure).
 Prove that

(i) $\triangle ABD \cong \triangle BAC$

(ii) $BD = AC$

$\angle \angle$

(iii) $\angle ABD = \angle BAC$



Answer:

In $\triangle ABD$ and $\triangle BAC$,

$AD = BC$ (Given)

$\angle \angle$

$\angle DAB = \angle CBA$ (Given)

$AB = BA$ (Common)

$\therefore \triangle ABD \cong \triangle BAC$ (By SAS congruence rule)

\therefore

$BD = AC$ (By CPCT) And, $\angle ABD$

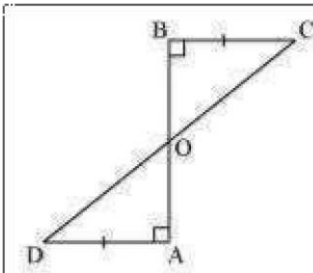
\angle

$= \angle BAC$ (By CPCT)

Question 3:

AD and BC are equal perpendiculars to a line segment AB (See the given figure).

Show that CD bisects AB.



Answer:

In $\triangle BOC$ and $\triangle AOD$,

\angle

\angle

$\angle BOC = \angle AOD$ (Vertically opposite angles)

$\angle CBO = \angle DAO$ (Each 90°)

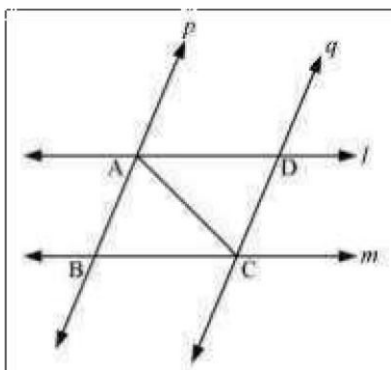
$BC = AD$ (Given)

$\therefore \triangle BOC \cong \triangle AOD$ (AAS congruence rule) $BO = AO$ (By CPCT)

\Rightarrow CD bisects AB.

Question 4: l and m are two parallel lines intersected by another pair of parallel lines p and q (see

the given figure). Show that $\triangle ABC \cong \triangle CDA$.



Answer:

In $\triangle ABC$ and $\triangle CDA$,
 $\angle BAC = \angle DCA$ (Alternate interior angles, as $p \parallel q$)

$AC = CA$ (Common)

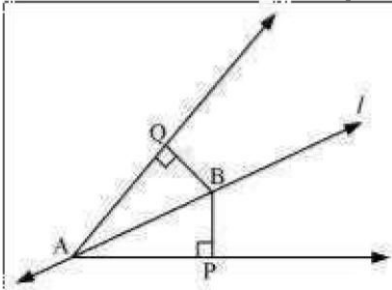
$\angle BCA = \angle DAC$

$\therefore \triangle BCA \cong \triangle DAC$ (Alternate interior angles, as $l \parallel m$)
 $\triangle ABC \cong \triangle CDA$ (By ASA congruence rule)

Question 5:

Line l is the bisector of an angle and B is any point on l . BP and BQ are perpendiculars from B to the arms of the angle (see the given figure). Show that: i) $\triangle APB \cong \triangle AQB$

(ii) $BP = BQ$ or B is equidistant from the arms of the angle.



Answer:

In $\triangle APB$ and $\triangle AQB$,

$\sphericalangle APB = \sphericalangle AQB$

$\sphericalangle PAB = \sphericalangle QAB$ (Each 90°)
 $\sphericalangle PAB = \sphericalangle QAB$ (l is the angle bisector of $\sphericalangle A$)

$AB = AB$ (Common)

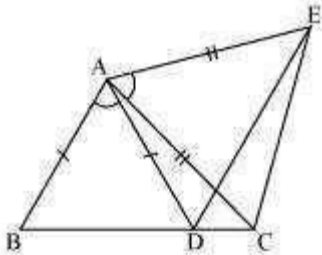
$\therefore \triangle APB \cong \triangle AQB$ (By AAS congruence rule) $\therefore BP = BQ$
 (By CPCT)

rays of $\sphericalangle A$. Or,

it can be said that B is equidistant from the a

Question 6:

In the given figure, $AC = AE$, $AB = AD$ and $\sphericalangle BAD = \sphericalangle EAC$. Show that $BC = DE$.



Answer:

It is given that $\sphericalangle BAD = \sphericalangle EAC$

$\sphericalangle BAD + \sphericalangle DAC = \sphericalangle EAC + \sphericalangle DAC$

$\sphericalangle BAC = \sphericalangle DAE$

In $\triangle BAC$ and $\triangle DAE$, $AB = AD$

(Given) $\sphericalangle BAC =$

$\sphericalangle DAE$ (Proved above)

$AC = AE$ (Given)

\therefore

$\therefore \triangle BAC \cong \triangle DAE$ (By SAS congruence rule)

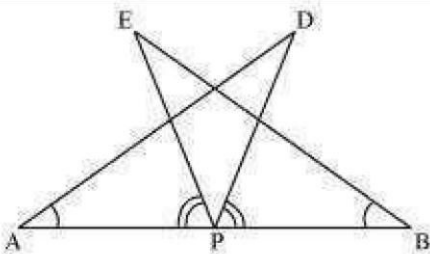
$BC = DE$ (By CPCT)

Question 7:

AB is a line segment and P is its mid-point. D and E are points on the same side of AB such that $\angle DAP = \angle EBP$ and $\angle EPA = \angle DPB$ (See the given figure). Show that i)

$\triangle DAP \cong \triangle EBP$ (

(ii) $AD = BE$



Answer:

It is given that $\angle EPA = \angle DPB$

$\therefore \angle EPA + \angle DPE = \angle DPB + \angle DPE$

$\therefore \angle DPA = \angle EPB$

In $\triangle DAP$ and $\triangle EBP$,

$\angle DPA = \angle EPB$ (Given)

$AP = BP$ (P is mid-point of AB)

\therefore

$\therefore \angle DPA = \angle EPB$ (From above)

$\therefore \triangle DAP \cong \triangle EBP$ (ASA congruence rule)

$\therefore AD = BE$ (By CPCT)

Question 8:

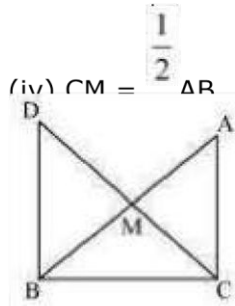
In right triangle ABC, right angled at C, M is the mid-point of hypotenuse AB. C is joined to M and produced to a point D such that $DM = CM$. Point D is joined to point

B (see the given figure). Show that: i)

$\triangle AMC \cong \triangle BMD$ (

ii) $\angle DBC$ is a right angle. (iii)

$\triangle DBC \cong \triangle ACB$ (



Answer:

(i) In $\triangle AMC$ and $\triangle BMD$,
 $AM = BM$ (M is the mid-point of AB)

$\angle AMC = \angle BMD$ (Vertically opposite angles)

$CM = DM$ (Given)

$\therefore \triangle AMC \cong \triangle BMD$ (By SAS congruence rule)

$\therefore AC = BD$ (By CPCT) And,

$\angle ACM = \angle BDM$ (By CPCT) ii)

$\therefore \angle ACM = \angle BDM$ (

)

However, $\angle ACM$ and $\angle BDM$ are alternate interior angles.

Since alternate angles are equal,

It can be said that $DB \parallel AC$

$\therefore \angle DBC + \angle ACB = 180^\circ$ (Co-interior angles)

$\therefore \angle DBC + 90^\circ = 180^\circ$ $\angle DBC$

$\therefore \angle DBC = 90^\circ$

(iii) In $\triangle DBC$ and $\triangle ACB$,

$DB = AC$ (Already proved)

$\angle DBC = \angle ACB$ (Each 90°)

$BC = CB$ (Common)

$\therefore \triangle DBC \cong \triangle ACB$ (SAS congruence rule) iv)

)

$\triangle DBC \cong \triangle ACB$ (

\therefore

$\therefore AB = DC$ (By CPCT)

$AB = 2 \text{ CM}$

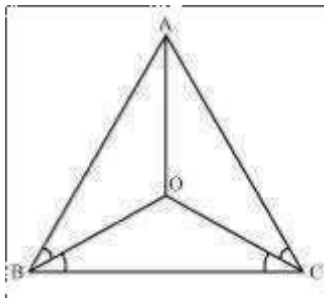
$\therefore \text{CM} = \frac{1}{2} AB$

Exercise 7.2 Question

1:

In an isosceles triangle ABC, with $AB = AC$, the bisectors of $\angle B$ and $\angle C$ intersect each other at O. Join A to O. Show that:

i) $OB = OC$ (ii) AO bisects $\angle A$ (Answer:



(i) It is given that in triangle ABC, $AB = AC$

$\therefore \angle C$

$\angle B$

$\angle C = \angle B$ (Angles opposite to equal sides of a triangle are equal)

$\therefore \frac{1}{2} \angle C$

$\frac{1}{2} \angle B$

$\therefore \angle OCB = \angle OBC$

$\therefore OB = OC$

\therefore

$OB = OC$ (Sides opposite to equal angles of a triangle are also equal)

(ii) In $\triangle OAB$ and $\triangle OAC$, $AO = AO$ (Common)

$AB = AC$ (Given)

$OB = OC$ (Proved above)

$\therefore \triangle OAB \cong \triangle OAC$ (By SSS congruence rule)

\therefore

$\angle BAO = \angle CAO$

Therefore, $\triangle OAB \cong \triangle OAC$ (By SSS congruence rule)

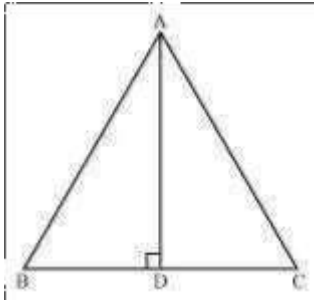
\therefore

$\angle BAO = \angle CAO$ (CPCT)

AO bisects $\angle A$.

Question 2:

In $\triangle ABC$, AD is the perpendicular bisector of BC (see the given figure). Show that $\triangle ABC$ is an isosceles triangle in which $AB = AC$.



Answer:

In $\triangle ADC$ and $\triangle ADB$,

$AD = AD$ (Common)

$\angle ADC = \angle ADB$ (Each 90°)

$CD = BD$ (AD is the perpendicular bisector of BC)

\therefore

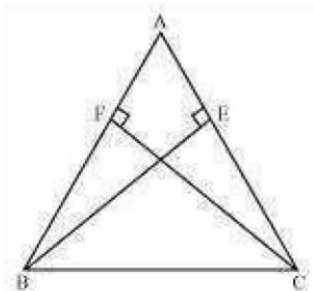
$\triangle ADC \cong \triangle ADB$ (By SAS congruence rule)

$AB = AC$ (By CPCT)

Therefore, $\triangle ABC$ is an isosceles triangle in which $AB = AC$.

Question 3:

$\triangle ABC$ is an isosceles triangle in which altitudes BE and CF are drawn to equal sides AC and AB respectively (see the given figure). Show that these altitudes are equal.



Answer:

In $\triangle AEB$ and $\triangle AFC$,

$\angle AEB$ and $\angle AFC$ (Each 90°) $\angle A =$

$\angle A$ (Common angle)

$AB = AC$ (Given)

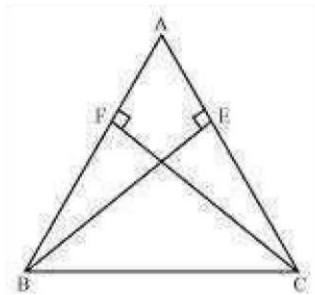
$\therefore \triangle AEB \cong \triangle AFC$ (By AAS congruence rule) $\therefore BE = CF$
(By CPCT)

Question 4:

ABC is a triangle in which altitudes BE and CF to sides AC and AB are equal (see the

given figure). Show that

(i) $\triangle ABE \cong \triangle ACF$



Answer:

(ii) $AB = AC$, i.e., ABC is an isosceles triangle.

(i) In $\triangle ABE$ and $\triangle ACF$,

$\angle ABE$ and $\angle ACF$ (Each 90°)

$\angle A = \angle A$ (Common angle)

$BE = CF$ (Given)

$\therefore \triangle ABE \cong \triangle ACF$ (By AAS congruence rule)

(ii) It has already been proved that

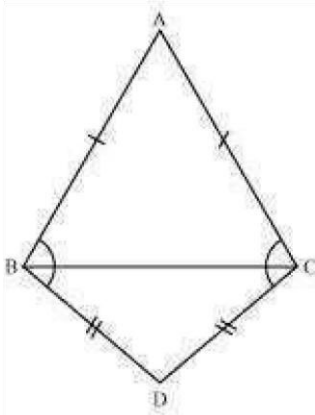
$\triangle ABE \cong \triangle ACF$

$\therefore AB = AC$ (By CPCT)

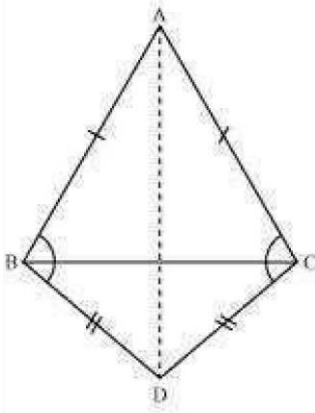
Question 5:

$\triangle ABC$ and $\triangle DBC$ are two isosceles triangles on the same base BC (see the given figure).

Show that $\angle ABD = \angle ACD$.



Answer:



Let us join AD.

In $\triangle ABD$ and $\triangle ACD$,

$AB = AC$ (Given)

$BD = CD$ (Given)

$AD = AD$ (Common side)

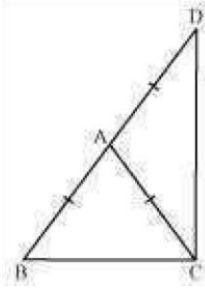
$\therefore \triangle ABD \cong \triangle ACD$

$\therefore \angle ABD = \angle ACD$ (By SSS congruence rule)

$\angle ABD = \angle ACD$ (By CPCT)

Question 6:

$\triangle ABC$ is an isosceles triangle in which $AB = AC$. Side BA is produced to D such that $AD = AB$ (see the given figure). Show that $\angle BCD$ is a right angle.



Answer:

In $\triangle ABC$,

$AB = AC$ (Given)

$\therefore \angle ACB = \angle ABC$ (Angles opposite to equal sides of a triangle are also equal)

In $\triangle ACD$,

$AC = AD$

$\therefore \angle ADC = \angle ACD$ (Angles opposite to equal sides of a triangle are also equal)

In $\triangle BCD$,

$\angle ABC + \angle BCD + \angle ADC = 180^\circ$ (Angle sum property of a triangle)

$\angle ACB + \angle ACB + \angle ACD + \angle ACD = 180^\circ$

$2(\angle ACB + \angle ACD) = 180^\circ$

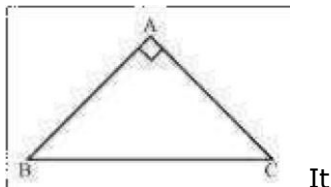
$2(\angle BCD) = 180^\circ$

$\angle BCD = 90^\circ$

Question 7:

ABC is a right angled triangle in which $\angle A = 90^\circ$ and $AB = AC$. Find $\angle B$ and $\angle C$.

Answer:



is given that

$AB = AC$

$\therefore \angle C = \angle B$ (Angles opposite to equal sides are also equal)

$\therefore \angle B = \angle C$

$\therefore \angle B = \angle C = 45^\circ$

In $\triangle ABC$,

$$A + B + C = 180^\circ \text{ (Angle sum property of a triangle)}$$

$$90^\circ + B + C = 180^\circ$$

$$90^\circ + B + B = 180^\circ$$

$$2 B = 90^\circ$$

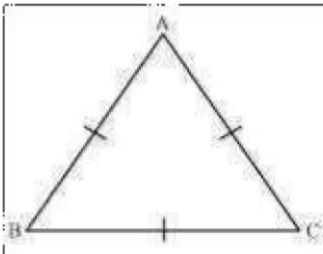
$$B = 45^\circ$$

$$B = C = 45^\circ$$

Question 8:

Show that the angles of an equilateral triangle are 60° each.

Answer:



Let us consider that ABC is an equilateral triangle.

Therefore, $AB = BC = AC$

$$AB = AC$$

$$\hat{C} = \hat{B} \text{ (Angles opposite to equal sides of a triangle are equal) Also,}$$

$$AC = BC$$

$$\hat{B} = \hat{A} \text{ (Angles opposite to equal sides of a triangle are equal)}$$

Therefore, we obtain \hat{A}

$$= \hat{B} = \hat{C}$$

In $\triangle ABC$,

$$\hat{A} + \hat{B} + \hat{C} = 180^\circ$$

$$A + A + A = 180^\circ$$

$$3 A = 180^\circ$$

$$A = 60^\circ$$

$A = B = C = 60^\circ$ Hence, in an equilateral triangle, all interior angles are of measure 60° .

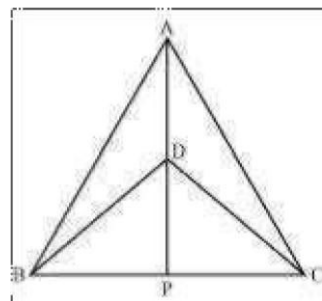
Exercise 7.3

Question 1:

$\triangle ABC$ and $\triangle DBC$ are two isosceles triangles on the same base BC and vertices A and D are on the same side of BC (see the given figure). If AD is extended to intersect

BC at P , show that

- i) $\triangle ABD \cong \triangle ACD$ (ii) $\triangle ABP \cong \triangle ACP$
 (iii) AP bisects $\angle A$ as well as D . (
 (iv) AP is the perpendicular bisector of BC .



Answer:

(i) In $\triangle ABD$ and $\triangle ACD$,

$AB = AC$ (Given)

$BD = CD$ (Given)

$AD = AD$ (Common)

$\therefore \triangle ABD \cong \triangle ACD$ (By SSS congruence rule)

$\therefore \angle BAD = \angle CAD$ (By CPCT)

$\therefore AP$ bisects $\angle A$

$$\angle BAP = \angle CAP \dots (1)$$

(ii) In $\triangle ABP$ and $\triangle ACP$,

$$AB = AC \text{ (Given)}$$

$$\angle BAP = \angle CAP \text{ [From equation (1)]}$$

$$AP = AP \text{ (Common)}$$

\therefore

$\therefore \triangle ABP \cong \triangle ACP$ (By SAS congruence rule)

$$BP = CP \text{ (By CPCT) } \dots (2)$$

(iii) From equation (1),

$$\angle BAP = \angle CAP$$

Hence, AP bisects $\angle A$.

In $\triangle BDP$ and $\triangle CDP$,

$$BD = CD \text{ (Given)}$$

$$DP = DP \text{ (Common)}$$

$$BP = CP \text{ [From equation (2)]}$$

$\therefore \triangle BDP \cong \triangle CDP$ (By S.S.S. Congruence rule)

$$\angle BDP = \angle CDP \text{ (By CPCT) } \dots (3) \text{ Hence,}$$

AP bisects $\angle D$. iv) $\triangle BDP \cong \triangle CDP$

$\triangle CDP$ (

$$\angle BPD = \angle CPD \text{ (By CPCT) } \dots (4)$$

\therefore

$$\angle BPD + \angle CPD = 180^\circ \text{ (Linear pair angles)} \quad \angle BPD + \angle BPD = 180^\circ$$

\therefore

$$2\angle BPD = 180^\circ \text{ [From equation (4)]}$$

$$\angle BPD = 90^\circ \dots (5)$$

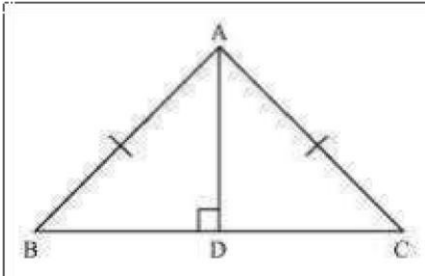
From equations (2) and (5), it can be said that AP is the perpendicular bisector of BC.

Question 2:

AD is an altitude of an isosceles triangles ABC in which $AB = AC$. Show that

i) AD bisects BC (ii) AD bisects $\angle A$. (

Answer:



(i) In $\triangle BAD$ and $\triangle CAD$,

$\angle ADB = \angle ADC$ (Each 90° as AD is an altitude)

$AB = AC$ (Given)

$AD = AD$ (Common)

\therefore

$\therefore \triangle BAD \cong \triangle CAD$ (By RHS Congruence rule)

$BD = CD$ (By CPCT)

Hence, AD bisects BC.

(ii) Also, by CPCT,

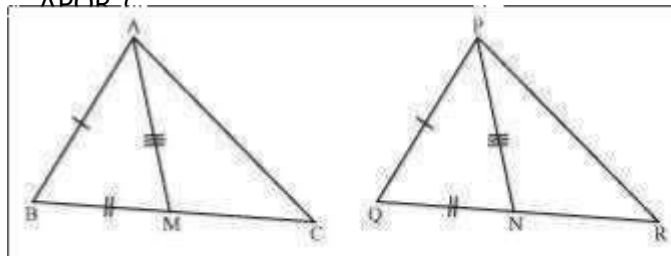
$\angle BAD = \angle CAD$ Hence, AD

bisects A.

Question 3:

Two sides AB and BC and median AM of one triangle ABC are respectively equal to sides PQ and QR and median PN of $\triangle PQR$ (see the given figure). Show that: i) $\triangle ABM$

$\Delta PQR \cong \Delta ABC$ (ii) $\Delta ABC \cong \Delta PQR$ (i)



∴ Answer:

(i) In ΔABC , AM is the median to BC.

$$\therefore BM = \frac{1}{2} BC$$

$$\therefore QN = \frac{1}{2} QR$$

However, $BC = QR$

$$\therefore \frac{1}{2} BC = \frac{1}{2} QR$$

$$\therefore BM = QN \dots (1)$$

In ΔABM and ΔPQN , In ΔPQR , PN is the median to QR.

$$AB = PQ \text{ (Given)}$$

$$BM = QN \text{ [From equation (1)]}$$

$$AM = PN \text{ (Given)}$$

∴ $\Delta ABM \cong \Delta PQN$ (SSS congruence rule)

∴ $\angle ABM = \angle PQN$ (By CPCT)

∴ $\angle ABC = \angle PQR \dots (2)$

(ii) In ΔABC and ΔPQR ,

$$AB = PQ \text{ (Given)}$$

$$\angle ABC = \angle PQR \text{ [From equation (2)]}$$

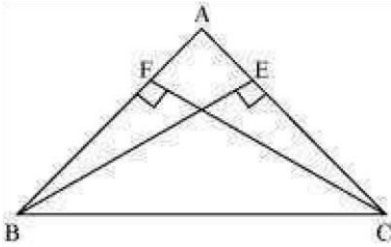
$$BC = QR \text{ (Given)}$$

∴ $\Delta ABC \cong \Delta PQR$ (By SAS congruence rule)

Question 4:

BE and CF are two equal altitudes of a triangle ABC. Using RHS congruence rule, prove that the triangle ABC is isosceles.

Answer:



In $\triangle BEC$ and $\triangle CFB$,

$\therefore \angle BEC = \angle CFB$ (Each 90°)

$BC = CB$ (Common)

$BE = CF$ (Given)

$\therefore \triangle BEC \cong \triangle CFB$ (By RHS congruency)

$\therefore \angle BCE = \angle CBF$ (By CPCT)

$\therefore AB = AC$ (Sides opposite to equal angles of a triangle are equal)

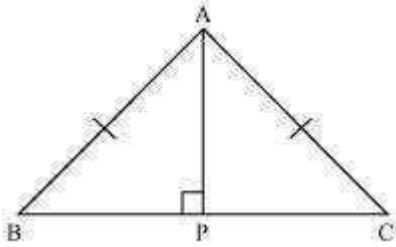
Hence, $\triangle ABC$ is isosceles.

Question 5:

$\therefore \therefore$

Answer:

ABC is an isosceles triangle with $AB = AC$. Draw $AP \perp BC$ to show that $\angle B = \angle C$.



In $\triangle APB$ and $\triangle APC$,

$\angle APB = \angle APC$ (Each 90°)

$AB = AC$ (Given)

$AP = AP$ (Common)

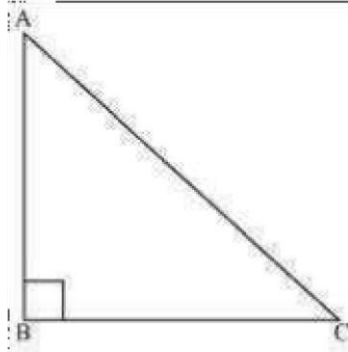
$\therefore \triangle APB \cong \triangle APC$ (Using RHS congruence rule)

$\therefore \angle B = \angle C$ (By using CPCT)

Exercise 7.4 Question 1:

Show that in a right angled triangle, the hypotenuse is the longest side.

Answer:



Let us consider a right-angled triangle ABC, right-angled at B.

In $\triangle ABC$,

$$\angle A + \angle B + \angle C = 180^\circ \text{ (Angle sum property of a triangle)}$$

$$\angle A + 90^\circ + \angle C = 180^\circ$$

$$\angle A + \angle C = 90^\circ$$

Hence, the other two angles have to be acute (i.e., less than 90°).

B is the largest angle in $\triangle ABC$.

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$$\therefore \therefore \quad \angle B > \angle A \text{ and } \angle B > \angle C$$

$$\therefore \therefore \quad \therefore \quad AC > BC \text{ and } AC > AB$$

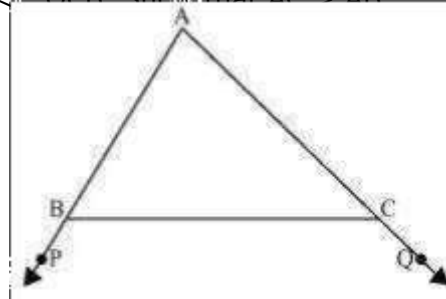
\therefore

[In any triangle, the side opposite to the larger (greater) angle is longer.]
Therefore, AC is the largest side in $\triangle ABC$.

However, AC is the hypotenuse of $\triangle ABC$. Therefore, hypotenuse is the longest side in a right-angled triangle.

Question 2:

In the given figure sides AB and AC of $\triangle ABC$ are extended to points P and Q respectively. Also, $\angle PBC < \angle QCB$. Show that $AC > AB$.



Answer:

In the given figure,

$$\angle ABC + \angle PBC = 180^\circ \text{ (Linear pair)}$$

$$\therefore \therefore \quad \angle ABC = 180^\circ - \angle PBC \dots (1)$$

Also,

\therefore

\therefore

$$\angle ACB + \angle QCB = 180^\circ$$

$$\angle ACB = 180^\circ - \angle QCB \dots (2)$$

As $\angle PBC < \angle QCB$,

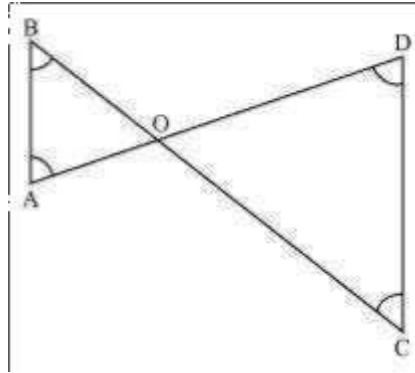
\therefore

$$\therefore \therefore 180^\circ - \angle PBC > 180^\circ - \angle QCB$$

$$\angle ABC > \angle ACB \text{ [From equations (1) and (2)] } \therefore AC >$$

AB (Side opposite to the larger angle is larger.) Question 3:

In the given figure, $\angle B < \angle A$ and $\angle C < \angle D$. Show that $AD < BC$.



Answer:

In $\triangle AOB$,

$$\because \angle B < \angle A \quad AO < BO \text{ (Side opposite to smaller angle is smaller) ... (1)}$$

In $\triangle COD$,

$$\because \angle C < \angle D$$

$$\therefore OD < OC \text{ (Side opposite to smaller angle is smaller) ... (2)}$$

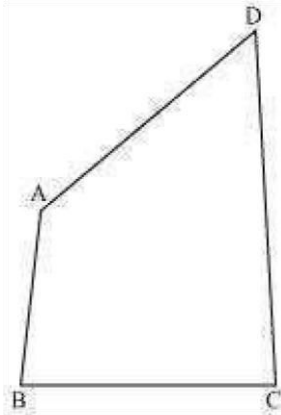
On adding equations (1) and (2), we obtain

$$AO + OD < BO + OC$$

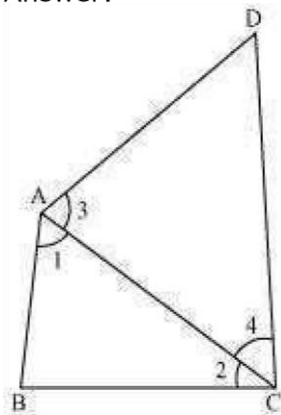
$$AD < BC$$

Question 4:

AB and CD are respectively the smallest and longest sides of a quadrilateral ABCD (see the given figure). Show that $\angle A > \angle C$ and $\angle B > \angle D$.



Answer:



Let us join AC.
In $\triangle ABC$,

$AB < BC$ (AB is the smallest side of quadrilateral ABCD)

$$\therefore \angle 2 < \angle 1 \text{ (Angle opposite to the smaller side is smaller) ... (1)}$$

In $\triangle ADC$,

$AD < CD$ (CD is the largest side of quadrilateral ABCD)

$$\therefore \angle 4 < \angle 3 \text{ (Angle opposite to the smaller side is smaller) ... (2)}$$

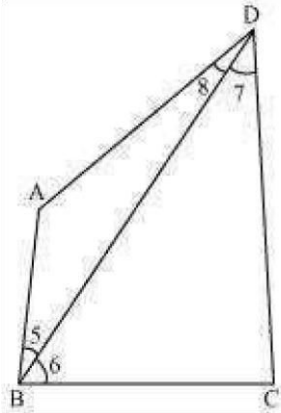
On adding equations (1) and (2), we obtain

$$\angle 2 + \angle 4 < \angle 1 + \angle 3$$

$$\angle C < \angle A$$

$$\angle A > \angle C$$

Let us join BD.



In $\triangle ABD$,

$AB < AD$ (AB is the smallest side of quadrilateral ABCD)

$$\angle 8 < 5 \text{ (Angle opposite to the smaller side is smaller) ... (3)}$$

In $\triangle BDC$,

$BC < CD$ (CD is the largest side of quadrilateral ABCD)

$$\angle 7 < \angle 6 \text{ (Angle opposite to the smaller side is smaller) ... (4)}$$

On adding equations (3) and (4), we obtain

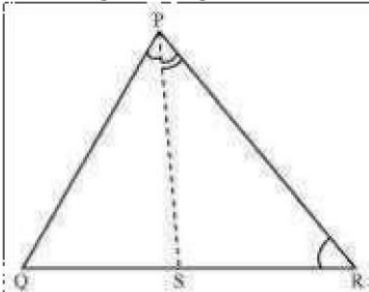
$$\angle 8 + \angle 7 < \angle 5 + \angle 6$$

$$\angle D < \angle B$$

$$\angle B > \angle D \text{ Question}$$

5:

In the given figure, $PR > PQ$ and PS bisects $\angle QPR$. Prove that $\angle PSR > \angle PSQ$.



Answer:

As $PR > PQ$,

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$\angle PQR > \angle PRQ$ (Angle opposite to larger side is larger) ... (1) PS is the bisector of QPR.

$$\angle QPS = \angle RPS \dots (2)$$

$\angle PSR$ is the exterior angle of $\triangle PQS$.

$$\angle PSR = \angle PQR + \angle QPS \dots (3)$$

$\angle PSQ$ is the exterior angle of $\triangle PRS$.

$$\angle PSQ = \angle PRQ + \angle RPS \dots (4)$$

Adding equations (1) and (2), we obtain

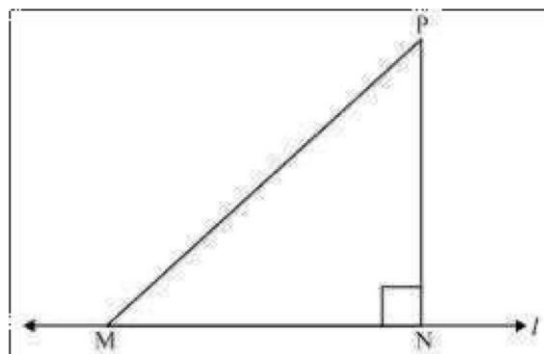
$$\angle PQR + \angle QPS > \angle PRQ + \angle RPS$$

$$\angle PSR > \angle PSQ \text{ [Using the values of equations (3) and (4)]}$$

Question 6:

Show that of all line segments drawn from a given point not on it, the perpendicular line segment is the shortest.

Answer:



Let us take a line l and from point P (i.e., not on line l), draw two line segments PN and PM . Let PN be perpendicular to line l and PM is drawn at some other angle.

In $\triangle PNM$,

$$\angle N = 90^\circ$$

$$\angle P + \angle N + \angle M = 180^\circ \text{ (Angle sum property of a triangle)}$$

$$\angle P + \angle M = 90^\circ$$

Clearly, $\angle M$ is an acute angle.

$$\angle M < \angle N$$

$PN < PM$ (Side opposite to the smaller angle is smaller)

Similarly, by drawing different line segments from P to l , it can be proved that PN is smaller in comparison to them.

Therefore, it can be observed that of all line segments drawn from a given point not on it, the perpendicular line segment is the shortest.

Exercise 7.5 Question

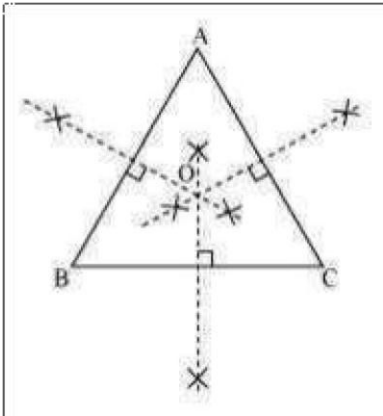
1:

ABC is a triangle. Locate a point in the interior of $\triangle ABC$ which is equidistant from all the vertices of $\triangle ABC$.

Answer:

Circumcentre of a triangle is always equidistant from all the vertices of that triangle.

Circumcentre is the point where perpendicular bisectors of all the sides of the triangle meet together.



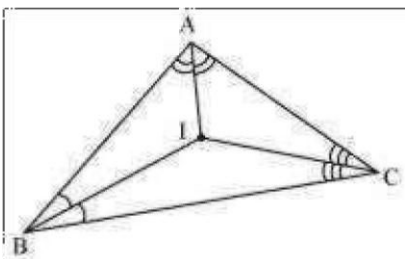
In $\triangle ABC$, we can find the circumcentre by drawing the perpendicular bisectors of sides AB, BC, and CA of this triangle. O is the point where these bisectors are meeting together. Therefore, O is the point which is equidistant from all the vertices of $\triangle ABC$.

Question 2:

In a triangle locate a point in its interior which is equidistant from all the sides of the triangle.

Answer:

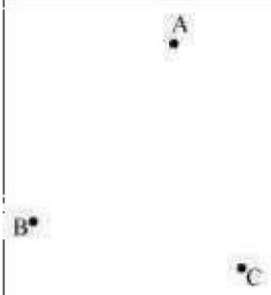
The point which is equidistant from all the sides of a triangle is called the incentre of the triangle. Incentre of a triangle is the intersection point of the angle bisectors of the interior angles of that triangle.



Here, in $\triangle ABC$, we can find the incentre of this triangle by drawing the angle bisectors of the interior angles of this triangle. I is the point where these angle bisectors are intersecting each other. Therefore, I is the point equidistant from all the sides of $\triangle ABC$.

Question 3:

In a huge park people are concentrated at three points (see the given figure)



A: where there are different slides and swings for children,

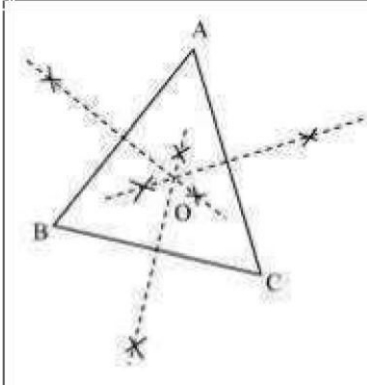
B: near which a man-made lake is situated,

C: which is near to a large parking and exit.

Where should an ice-cream parlour be set up so that maximum number of persons can approach it?

(Hint: The parlor should be equidistant from A, B and C) Answer:

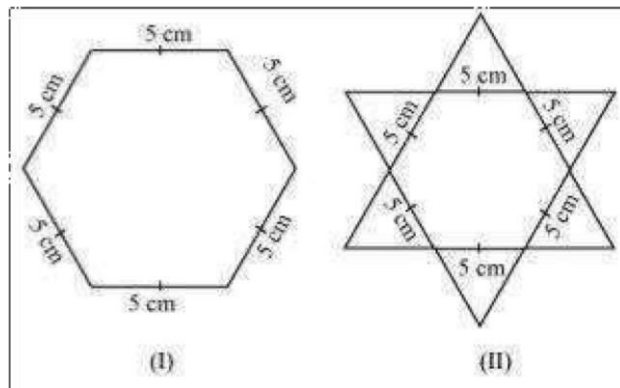
Maximum number of persons can approach the ice-cream parlour if it is equidistant from A, B and C. Now, A, B and C form a triangle. In a triangle, the circumcentre is the only point that is equidistant from its vertices. So, the ice-cream parlour should be set up at the circumcentre O of $\triangle ABC$.



In this situation, maximum number of persons can approach it. We can find circumcentre O of this triangle by drawing perpendicular bisectors of the sides of this triangle.

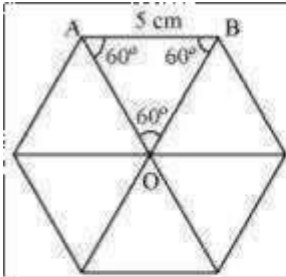
Question 4:

Complete the hexagonal and star shaped rangolies (see the given figures) by filling them with as many equilateral triangles of side 1 cm as you can. Count the number of triangles in each case. Which has more triangles?



Answer:

It can be observed that hexagonal-shaped rangoli has 6 equilateral triangles in it. ncrtsolutions.blogspot.com



$$= \frac{\sqrt{3}}{4} (\text{side})^2 = \frac{\sqrt{3}}{4} (5)^2$$

Area of ΔOAB

$$= \frac{\sqrt{3}}{4} (25) = \frac{25\sqrt{3}}{4} \text{ cm}^2$$

$$= 6 \times \frac{25\sqrt{3}}{4} = \frac{75\sqrt{3}}{2} \text{ cm}^2$$

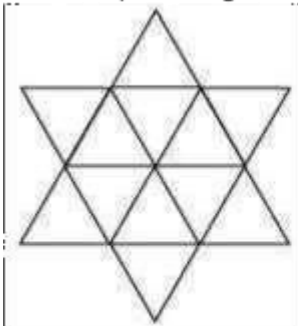
Area of hexagonal-shaped rangoli

$$\text{Area of equilateral triangle having its side as 1 cm} = \frac{\sqrt{3}}{4} (1)^2 = \frac{\sqrt{3}}{4} \text{ cm}^2$$

Number of equilateral triangles of 1 cm side that can be filled

$$\text{in this hexagonal-shaped rangoli} = \frac{\frac{75\sqrt{3}}{2}}{\frac{\sqrt{3}}{4}} = 150$$

Star-shaped rangoli has 12 equilateral triangles of side 5 cm in it.



$$\text{Area of star-shaped rangoli} = 12 \times \frac{\sqrt{3}}{4} \times (5)^2 = 75\sqrt{3}$$

Number of equilateral triangles of 1 cm side that can be filled

in this star-shaped *rangoli* = $\frac{75\sqrt{3}}{\frac{\sqrt{3}}{4}} = 300$

Therefore, star-shaped rangoli has more equilateral triangles in it.



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