

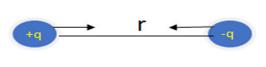
What is coulomb's law? | A detailed introduction

There are two types of <u>charges</u> positive and negative. Same charges repel each other. For example, if we have 2 negative or 2 positive charges then they will repel each other.

Opposite charges attract each other. It means if we have one positive and one negative charge or then there will be a force of attraction between them. This is the qualitative analysis of force between charges which tells us that there are two types of force between charges.

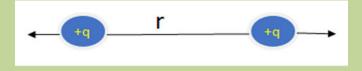
Force of Attraction





Representation of force of attraction

Force of Repulsion



Representation of force of repulsion

What is a point charge?

A charge is said to be a point charge when the distance between charges is far greater than their magnitude

Discovery of Coulomb's law

In 1786 AD Charles coulomb who was a French military engineer gave coulomb's law. This gives the quantitative analysis of force (attraction or repulsion). It is an empirical law and he deduces this law from many experiments.

When coulomb's law is applicable

Coulomb's law is only applicable when

- Charges should be static
- Charges must be point charges ation for everyone
- Charges are far enough so that strong nuclear force does not dominate over coulomb force

We know that the same charges repel each other but in an atom, there are protons in the nucleus and they have a positive charge on them.

They should repel each other as they have the same positive charge but they attract each other because when we bring the same charges very close to each other a strong nuclear force of attraction is produced between them. This force is very strong and dominates the force of repulsion. Coulomb's law does not hold in this condition.

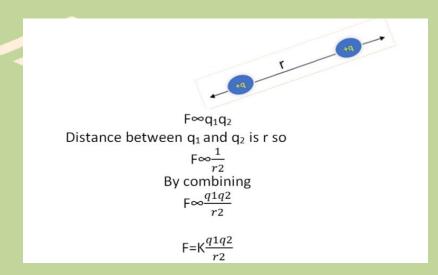
If we want to apply the coulomb's law on charges then there should be not any nuclear force between them.

Definition of coulomb's law

The force of attraction or repulsion between two static charges is directly proportional to the product of magnitudes of charges and inversely proportional to the square of the distance between them.

Mathematical derivation of coulomb's law

We suppose that we have two charges of magnitude q_1 and q_2 . And F is the force between them then according to coulomb's law.



K is the proportionality constant and is known as the coulomb's constant.

It is not a universal constant. Its values depend on

- Nature of medium between charges
- System of units

Unit of K

$$\mathsf{F=}\mathsf{K}\frac{q1q2}{r2}$$

$$K = \frac{Fr2}{q1q2}$$

By putting the units of F, r^2 , q_1 and q_2

$$K=Nm^2c^{-2}$$

Coulomb's law in free space or vacuum

The value of K is not fixed. The value of K is different in different mediums. The value of K for free space is not everyone

$$K = \frac{1}{4\pi\varepsilon o}$$

By putting this value in coulomb's formula

$$F = K \frac{q_1 q_2}{r_2}$$

$$F = \frac{1}{4\pi \varepsilon o} \frac{q_1 q_2}{r_2}$$

This is the coulomb's force in vacuum or free space and ϵ_o is the permittivity of free space.

What is permittivity?

<u>Permittivity</u> is taken from the word permeation. It means how much permeation is given by the medium to force to pass through it. But actually, permittivity means **How much does medium allow its own field to reduce the coulomb's forces**

Coulomb's force and permittivity have opposite relations.

$$F \infty \frac{1}{\varepsilon}$$

If the medium has more permittivity it will allow the coulomb's force to pass through it less. The value of permittivity for free space is 8.85×10⁻¹²N⁻¹m⁻²C². The value of K in free space is

$$K = \frac{1}{4\pi\varepsilon o}$$

By putting this value in coulomb's formula

$$F = K \frac{q_1 q_2}{r_2}$$

$$F = \frac{1}{4\pi \varepsilon o} \frac{q_1 q_2}{r_2}$$

The permittivity of free space is minimum so the maximum coulomb's force will pass through it.

If the permittivity of a medium is maximum then the coulomb's force will be minimum.

Coulomb's force in the medium

Coulomb's force depends on the permittivity of the medium and it varies with the medium between charges. If we want to find the coulomb's force in a particular medium then we compare the permittivity of that medium to the permittivity of space.

What is Relative permittivity?

The ratio between the permittivity of medium and space is called relative permittivity.

$$\varepsilon_r = \frac{\varepsilon m}{\varepsilon o}$$

Suppose the permittivity of the medium is ϵ_m then the force in that medium will be

$$F_{m} = \frac{1}{4\pi\epsilon m} \frac{q_{1}q_{2}}{r_{2}}$$
 The force in free space
$$F_{o} = \frac{1}{4\pi\epsilon o} \frac{q_{1}q_{2}}{r_{2}}$$
 By comparing these forces
$$\frac{Fo}{Fm} = \frac{\epsilon m}{\epsilon o}$$

$$As \epsilon_{r} = \frac{\epsilon m}{\epsilon o}$$

$$\frac{Fo}{Fm} = \epsilon_{r}$$

$$F_{m} = \frac{Fo}{\epsilon r}$$

It means that force in the medium is 1/st times the force in free space.

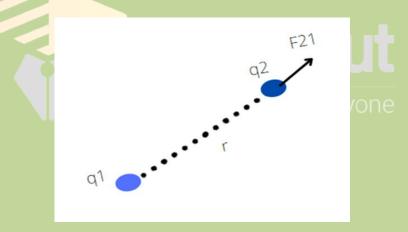
Since the permittivity of free space is minimum as compared to any medium so the force in free space will be maximum in free space than any other medium.

$$F_{o} > F_{m}$$

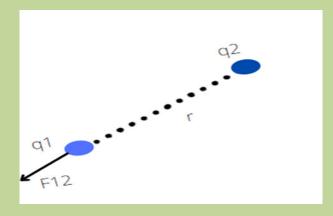
Vector form of coulomb's law

Coulomb's force is mutual force. According to Newton's third law when charge q_1 exerts a force on q_2 then at the same time q_2 also exerts a force on q_1 which is equal in magnitude but opposite in direction. This force act along the line joining the center of charges.

If the F₂₁ is a force on q₂ by q₁



 F_{12} is a force on q_1 by q_2



hen according to Newton's law

Force is a vector quantity. We multiply the unit vector with magnitude to find the vector quantity.

\hat{r}_{21} is the unit vector of F21

$$F_{21} = \frac{1}{4\pi\varepsilon o} \frac{q_1q_2}{r_2} \, \hat{r}_{21}$$
 Similarly
$$F_{12} = \frac{1}{4\pi\varepsilon o} \frac{q_1q_2}{r_2} \, \hat{r}_{12}$$
 As
$$F_{21} = -F_{12}$$
 By putting values
$$\hat{r}_{21} = -\hat{r}_{12}$$

It means the unit vectors are also the same in magnitude but opposite in direction. Now we solve some numerical related to coulomb's law.

Coulomb's Law: Problems and Solutions

1. Compute the electric force between two charges of 5×10^{-9} C and -3×10^{-8} C which are separated by

d = 10cm.

Solution:

The magnitude of the electrostatic force between two point charges is given by Coulomb's law as

$$F = k \frac{q^{1}q^{2}}{d^{2}}$$
By putting value
$$= (9 \times 10^{9}) (5 \times 10^{-9})(-3 \times 10^{-8})$$

$$(0.1)^{2}$$

$$= 135 \times 10^{-6} \text{ N}$$

2: Two spheres located at a distance of d = 5 cm attract one another with a force of F = 3 N. If one of them has three times more charges than the other, find the electric force between them.

Solution:

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$$q_1=?$$
 $q_2=3q_1$
According to coulomb law
 $F = k \frac{q_1q_2}{d_2}$
By putting value
 $3 = (9 \times 10^9) (\underline{q_1}) (3\underline{q_1})$
 $(0.5)^2$
 $q_1^2 = \underline{3 \times 0.0025}$
 $3 \times 9 \times 10^9$
 $q_1 = 1.6 \times 10^{-11}$